

(b)

1	(1)	R	A
2	(2)	P	A
1	(3)	$P \rightarrow R$	$1 \rightarrow I(2)$

(c)

1	(1)	P	A
	(2)	$P \rightarrow P$	$1 \rightarrow I(1)$

arrow-elim Given a conditional sentence (at line m) and another sentence that is its antecedent (at line n), conclude the consequent of the conditional.

Annotation: $m, n \rightarrow E$

Assumption set: The union of the assumption sets at lines m and n .

Comment: The order of m and n in the proof is irrelevant.

Also known as: Modus Ponendo Ponens (MPP), Modus Ponens (MP), Detachment, Affirming the Antecedent.

Example.

1	(1)	$P \rightarrow Q$	A
2	(2)	P	A
1,2	(3)	Q	$1,2 \rightarrow E$